mation
9–1)
/2H
Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You must show all your working.
- Diagrams are **NOT** accurately drawn, unless otherwise indicated.
- Calculators may be used.
- If your calculator does not have a π button, take the value of π to be 3.142 unless the question instructs otherwise.

Information

- The total mark for this paper is 80
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.



Turn over ▶







Please note that these worked solutions have neither been provided nor approved by Pearson Education and may not necessarily constitute the only possible solutions. Please refer to the original mark schemes for full guidance.

Any writing in blue indicates what must be written in order to answer the questions and get the marks. The worked solutions have been designed to show the smallest amount of work which needs to be done to answer the question.

Anything written in green in a cloud doesn't have to be written in the exam.

Anything written in orange in a rectangle doesn't have to be written in the exam and is there to show what should be put into a calculator or measured using a ruler or protractor.

If you find any mistakes or have any requests or suggestions, please send an email to curtis@cgmaths.co.uk

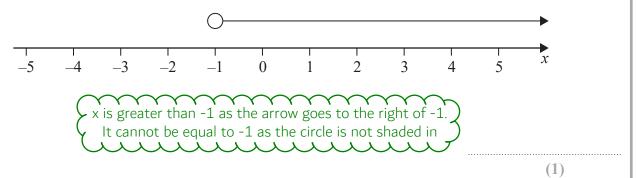
.CG Maths.

Answer ALL questions.

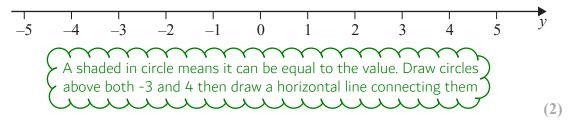
Write your answers in the spaces provided.

You must write down all the stages in your working.

1 (a) Write down the inequality shown on this number line.



(b) On the number line below, show the inequality $-3 \le y < 4$



(Total for Question 1 is 3 marks)

2 (a) Find the Highest Common Factor (HCF) of 60 and 84

Use the calculator to express 60 and 84 as a product of prime factors

➤ The lowest power of each prime in both

Iists multiplied together gives the HCF ✓

If using a Casio fx-85GT CW, go to CATALOG, Numeric Calc then GCD. GCD(60, 84)

(2)

(b) Find the Lowest Common Multiple (LCM) of 24 and 40

Use the calculator to express 24 and 40 as a product of prime factors

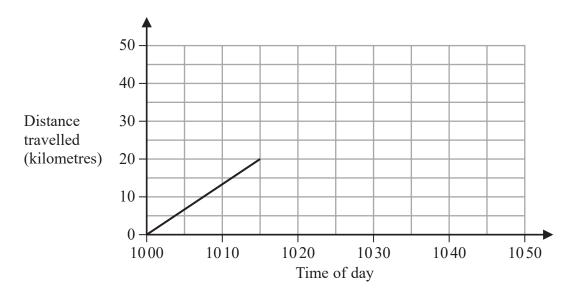
The highest power of each prime in both lists multiplied together gives the LCM <

If using a Casio fx-85GT CW, go to CATALOG, Numeric Calc then LCM. LCM(24, 40)

(2)

(Total for Question 2 is 4 marks)

3 Sam drives his car on a journey. Here is the travel graph for the first 15 minutes of his journey.



(a) Work out Sam's speed, in km/h, for the first 15 minutes of his journey.



Time can be entered into the calculator using the vin button

..... km/h

At 1015 Sam stops for 10 minutes and then drives for 20 minutes at a speed of 75 km/h.

(b) On the grid, complete the travel graph for Sam's journey.

If stopped, distance does not change. Work out what extra distance Sam does in the 20 minutes

From the formula triangle, distance = speed x time. The speed is 75km/h and the time is 20 minutes. Time can be entered into the calculator using the "" button

(3)

(Total for Question 3 is 5 marks)

4 (a) Complete the table of values for $y = x^2 - 2x + 2$

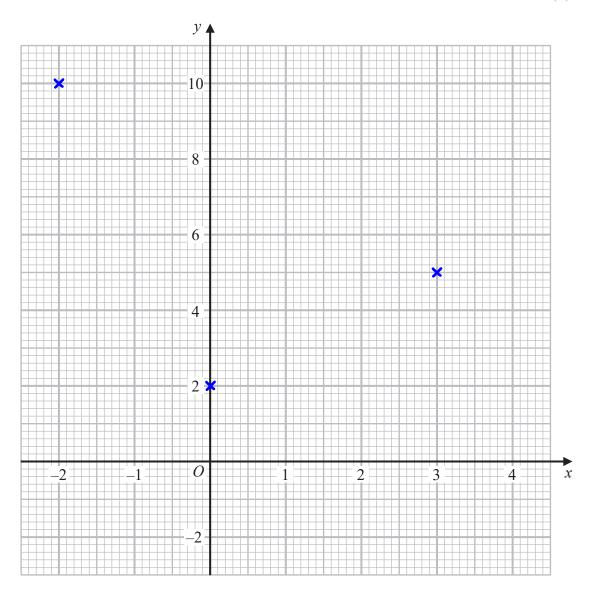
x	-2	-1	0	1	2	3	4
y	10		2			5	

Use table mode. Define $f(x) = x^2 - 2x + 2$. Table range start: -2, end: 4, step: 1

(b) On the grid, draw the graph of $y = x^2 - 2x + 2$ for values of x from -2 to 4

(2)

(2)



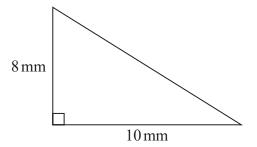
(c) Use your graph to find estimates of the solutions of the equation $x^2 - 2x + 2 = 4$



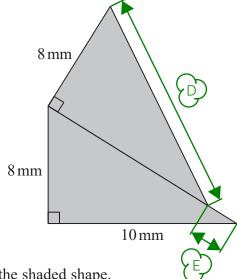
(2)

(Total for Question 4 is 6 marks)

5 Here is a right-angled triangle.



The shaded shape below is made from two of these triangles.



Work out the perimeter of the shaded shape. Give your answer correct to 3 significant figures.

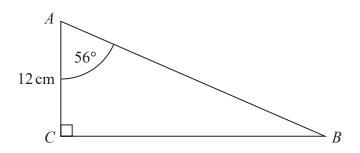
Pythgoras' Theorem can be used to work out the longest side of the right angled traingle. c is the longest side

Perimeter is all of the outside edges added together. To give the answer as a decimal to 3 significant figures, use the fourth figure to round the third then ignore everything after the third figure

..... mm

(Total for Question 5 is 4 marks)

6 ABC is a right-angled triangle.



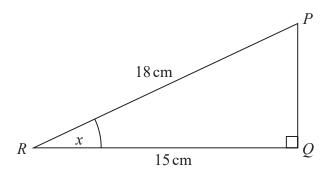
(a) Work out the length of *BC*. Give your answer correct to 1 decimal place.

Right angled trigonometry can be used to work out side BC.

Tick what we have and what we are looking for. Two ticks on a formula triangle means that one can be used. Covering what we are looking for in a formula triangle gives how to find it

(2)

PQR is a right-angled triangle.



(b) Work out the size of the angle marked *x*. Give your answer correct to 1 decimal place.

Right angled trigonometry can be used to work out angle x. Tick what we have. Two ticks on a formula triangle means that one can be used. Covering what we are looking for in a formula triangle gives how to find it. An inverse trig function will be necessary

(2)

(Total for Question 6 is 4 marks)

7 Liquid **A** has a density of 1.8 g/cm³ Liquid **B** has a density of 1.2 g/cm³

 $80\,\mathrm{cm^3}$ of liquid **A** is mixed with $40\,\mathrm{cm^3}$ of liquid **B** to make $120\,\mathrm{cm^3}$ of liquid **C**.

Work out the density of liquid C.



The mass of C can be found by adding the masses of A and B

g	cm/
---	-----

(Total for Question 7 is 3 marks)

8 The grouped frequency table gives information about the time, in minutes, taken by 50 people to solve a puzzle.

Time (t minutes)	Frequency
$0 < t \leqslant 10$	5
$10 < t \leqslant 20$	8
$20 < t \leqslant 30$	12
$30 < t \leqslant 40$	15
$40 < t \leqslant 50$	7
$50 < t \leqslant 60$	3

Brian was asked to draw a cumulative frequency table for this information.

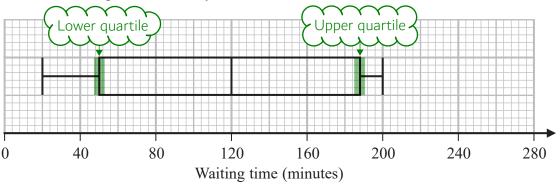
This is the table that Brian drew.

Time (t minutes)	Cumulative frequency
$0 < t \leqslant 10$	5
$10 < t \leqslant 20$	13
$20 < t \leqslant 30$	25
$30 < t \leqslant 40$	40
$40 < t \leqslant 50$	47
$50 < t \leqslant 60$	50

Write down **one** thing that is wrong with this cumulative frequency table.

(Total for Question 8 is 1 mark)

9 The box plot shows information about the length of time, in minutes, some people waited to see a doctor at a hospital on Monday.



(a) Work out the interquartile range of the information in the box plot.



Becky says,

"50% of the people waited for at least 2 hours."

(b) Is Becky correct? Explain why.

There are 60 minutes in an hour and 120/60 = 2 so 120 minutes is 2 hours. The median is halfway through the data and 50% is half

(1)

The table gives information about the length of time, in minutes, some people waited to see a doctor at the same hospital on Tuesday.

	Waiting time (minutes)
Shortest time	20
Lower quartile	50
Median	100
Upper quartile	140
Longest time	210

Becky was asked to compare the distribution of the lengths of times people waited on Monday with the distribution of the lengths of times people waited on Tuesday.

She wrote,

"People had to wait longer on Tuesday than on Monday."

(c) Give **one** reason why Becky may be wrong.



(1)

(Total for Question 9 is 4 marks)

10 Louise invests £x in Better Investments for 3 years. Sadiq invests £x in County Bank for 3 years.

Better Investments

Compound Interest

2.5% per annum

County Bank

Compound Interest

2% per annum for the first two years 3.5% per annum for each extra year

At the end of the 3 years, the value of Louise's investment is £344605

Work out the value of Sadiq's investment at the end of the 3 years.

$$\propto \times \left(\frac{100 + 2.5}{100}\right)^3 = 344605$$

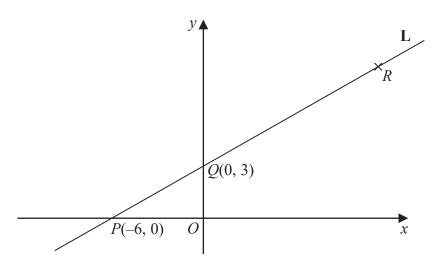
100 + 2.5 works out the percentage Louise's investment rises to each year. Dividing this by 100 converts it into a multiplier which when multiplied by increases by 2.5%. Multiplying x by this to the power of 3 increases x by 2.5% 3 times, which must be equal to the value of the investment at the end of 3 years

Rearrange to find x then apply the interest to it for Sadiq's investment

f

(Total for Question 10 is 4 marks)

11 Here is a sketch of the line L.



The points P(-6, 0) and Q(0, 3) are points on the line L.

The point R is such that PQR is a straight line and PQ:QR=2:3

(a) Find the coordinates of R.

Works out the distance in the x direction from P to Q. Dividing this by 2 works out what 1 part of the ratio is worth in the x direction. Multiplying this by 3 works out what the distance is in the x direction from Q to R. Add this to the x coordinate of Q to get the x coordinate of R. Do a similar method for the y coordinates

(.....

(b) Find an equation of the line that is perpendicular to L and passes through Q.

The general equation of a straight line is y = mx + c, where m is the gradient and c is the y-intercept. The gradients of perpendicular lines are the negative reciprocal of each other. Gradient = (change in y)/(change in x). Change in y is found by subtracting the y coordinates of two points on the line from each other. Change in x is found by subtracting the x coordinates of two points on the line from each other in the same order. The y-intercept is given at point Q

(3)

(Total for Question 11 is 5 marks)

12 Expand and simplify (x-2)(3x+2)(2x+3)

Expand out the first two brackets. Simplify the result then expand this out with the third bracket. Simplify the result

(Total for Question 12 is 3 marks)

13 In a school there are 16 teachers and 220 students. Of these students 120 are girls and 100 are boys.

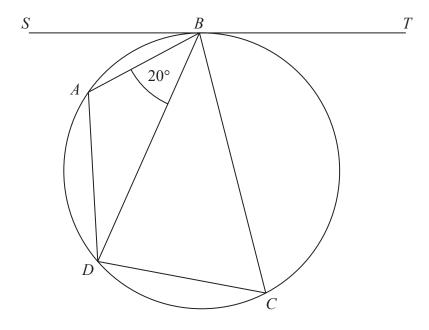
One teacher, one girl and one boy are going to be chosen to represent the school.

Work out the number of different ways there are to choose one teacher, one girl and one boy.

Use the product rule for counting. Multiplying the number of possibilities for each individual event gives the total number of possibilities

(Total for Question 13 is 2 marks)

14



A, B, C and D are four points on a circle. SBT is a tangent to the circle. Angle $ABD = 20^{\circ}$

the size of angle BAD: the size of angle BCD = 3:1

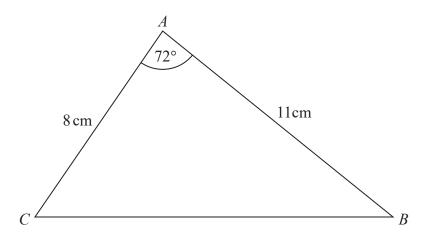
Find the size of angle *SBA*. Give a reason for each stage of your working.

Opposite angles in a cyclic quadrilateral add up to 180. So angles BAD and BCD must be 180 in total. This can be divided into the ratio to work out angle BCD. The alternate segment theorem (the angle between a tangent and a chord is equal to the interior opposite angle) can be used to work out angle SBD. Then angle SBA can be worked out

(Total for Question 14 is 4 marks)

15

15 Here is triangle *ABC*.



(a) Find the length of *BC*. Give your answer correct to 3 significant figures.

 $a^2 = b^2 + c^2 - 2bc \cos A \leftarrow$

It is not a right angled triangle so Pythagoras' theorem and right angled trigonometry cannot be used. There is not at least two opposite pairs of sides and angles and no other angles can be easily worked out so the sine rule cannot be used. The cosine rule must be used

Label the triangle with angle A (which must be the angle we have) then label the sides a, b and c. a is opposite A. Rearrange the cosine rule to make what we are looking for the subject then substitute in the values to find it

(3)

(b) Find the area of triangle *ABC*. Give your answer correct to 3 significant figures.

Area of triangle = 1/2 absinC, where a and b are two sides and C is the angle between them

 	cm ²
(2)	

(Total for Question 15 is 5 marks)

16 (a) Use the iteration formula $x_{n+1} = \sqrt[3]{10 - 2x_n}$ to find the values of x_1 , x_2 and x_3 Start with $x_0 = 2$

Enter 2 into the calculator then press = (or EXE) then enter $\sqrt[3]{10 - 2}$ ANS. Pressing =/EXE once gives x_1 , pressing it again gives x_2 , then pressing it again gives x_3

This works as it substitutes in the previous iteration of x into the formula to find the next iteration of x. x_{n+1} means the next iteration of x and x_n means the current iteration of x.

	$x_1 =$	
The values can be rounded to 2 decimal places	$\rightarrow x_2 =$	
	$\chi_{2} =$	
	-3	(3)

The values of x_1 , x_2 and x_3 found in part (a) are estimates of the solution of an equation of the form $x^3 + ax + b = 0$ where a and b are integers.

(b) Find the value of a and the value of b.

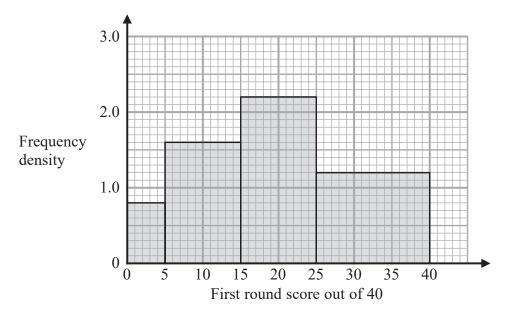
This must be what the iterative formula is derived from

Eliminate the cube root then rearrange into the desired form a = b = b

(Total for Question 16 is 4 marks)

17 Some people took part in the first round of a competition.

The histogram gives information about the scores of these people in the first round.



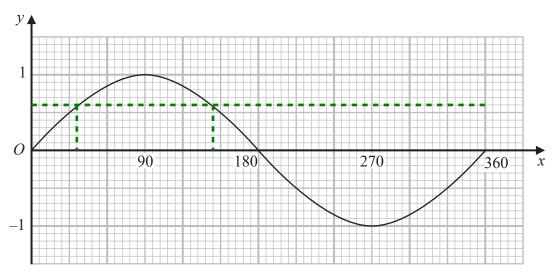
20% of the people got a score high enough for them to qualify for the second round.

Work out an estimate for the score needed to qualify for the second round. You must show all your working.

Frequency on a histogram is the area of each box. Frequency = class width x frequency density. The class width is how wide each box is and is found by finding the difference between the highest and lowest value of each box. Work out the total frequency, which is how many people there were, then do 20% of this to work out how many people qualified. Work out which class the lowest of the top 20% is in then assume that the scores are equally spread through the class and do the fraction of the way through the class from the end it is of the class width of that class then subtract this from the highest value in that class to find the estimate

(Total for Question 17 is 4 marks)

18 Here is a graph of $y = \sin x^{\circ}$ for $0 \le x \le 360$



(a) Using this graph, find estimates of all four solutions of

$$\sin x^{\circ} = 0.6 \quad \text{for } 0 \leqslant x \leqslant 720$$

$$\text{from } 360 < x < 720 \text{ so adding } 360 \text{ to each of } 160 \text{ t$$

The graph repeats from $360 \le x \le 720$ so adding 360 to each of the solutions on the graph given works out the solutions within this range

(2)

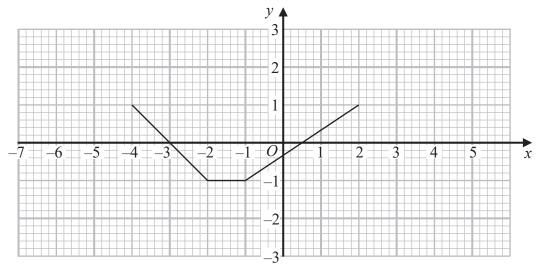
The graph of $y = \sin x^{\circ}$ is reflected in the *x*-axis.

(b) Write down an equation of the reflected graph.

y = -f(x) is a reflection in the x-axis as all of the positive values become negative and all of the negative values become positive

(1)

Here is a graph of y = f(x)



(c) On the grid, draw the graph of y = f(x - 2)

The graph translates 2 to the right as the same values are got to 2 later

(Total for Question 18 is 4 marks)

19 A, B and C are three spheres.

The volume of sphere **A** is 125 cm³ The volume of sphere **B** is 27 cm³

The ratio of the radius of sphere $\bf B$ to the radius of sphere $\bf C$ is 1:2

Work out the ratio of the surface area of sphere A to the surface area of sphere C.

The ratio of the volumes of A and B is 125: 27. The unit of volume is cm³. The unit of length is cm. So to go from the ratio of volume to the ratio of length, both sides need to be cube rooted. The unit of area is cm². So to go from the ratio of length to the ratio of area, both sides need to be squared. Also squaring the ratio of the lengths of B and C (radius is a length) gives the ratio of their areas. Write the ratio of the areas of A: B and B: C over each other then combine them by making the same number of parts for B. Then ignore B and write the ratio of A: C

(Total for Question 19 is 3 marks)

20 In a village,

if it rains on one day, the probability that it will rain on the next day is 0.8 if it does **not** rain on one day, the probability that it will rain on the next day is 0.6

A weather forecaster says,

"There is a 70% chance that it will rain in the village on Monday."

Work out an estimate for the probability that it will rain in the village on Wednesday. You must show all your working.

RRR, RNR, +

Systematically listing the possibilities for it to rain on Wednesday. Rain Monday AND rain Tuesday AND rain Wednesday OR Rain Monday AND not rain Tuesday AND rain Wednesday OR...

AND means to multiply the probabilities and OR means to add the probabilities

(Total for Question 20 is 4 marks)

21 The time period, T seconds, of a simple pendulum of length lcm is given by the formula

$$T = 2\pi \sqrt{\frac{l}{g}}$$

Katie uses a simple pendulum in an experiment to find an estimate for the value of g.

Here are her results.

l = 52.0 correct to 3 significant figures.

T = 1.45 correct to 3 significant figures.

Work out the upper bound and the lower bound for the value of *g*.

Use $\pi = 3.142$

You must show all your working.

Rearrange to make g the subject. Follow BIDMAS backward and do the opposite operations to both sides to eliminate everything apart from g from the right. At some point we need to do the reciprocal of both sides as g is the denominator. Then substitute in bounds of I and T to work out the upper bound and lower bound of g. When considering which bound to use, consider that one of the variables should be a denominator and dividing by more gives a smaller answer. To find the upper bound of one of the measurements, add half of the resolution. To find the lower bound of one of the measurements, subtract half of the resolution. The resolution of I is 0.1 as the third significant figure is in the first decimal place, which goes up in 0.1s

upper bound =	
lower bound =	

(Total for Question 21 is 4 marks)

TOTAL FOR PAPER IS 80 MARKS