

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

GCSE MATHEMATICS

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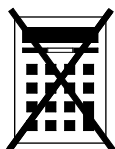
Higher Tier Paper 1 Non-Calculator

Tuesday 6 November 2018 Morning Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- mathematical instruments



You must **not** use a calculator.

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
TOTAL	

Advice

In all calculations, show clearly how you work out your answer.



Please note that these worked solutions have neither been provided nor approved by AQA and may not necessarily constitute the only possible solutions. Please refer to the original mark schemes for full guidance.

Any writing in blue indicates what must be written in order to answer the questions and get the marks. The worked solutions have been designed to show the smallest amount of work which needs to be done to answer the question.

Anything written in green in a cloud doesn't have to be written in the exam.

Anything written in orange in a rectangle doesn't have to be written in the exam and is there to show what should be put into a calculator or measured using a ruler or protractor.

If you find any mistakes or have any requests or suggestions, please send an email to curtis@cgmaths.co.uk

Answer **all** questions in the spaces provided

- 1 Simplify $(5^4)^2$
Circle your answer.

[1 mark]

5^6

5^8

25^6

25^8

$(a^x)^y = a^{xy}$
So multiply the powers together

- 2 Circle the volume, in cm^3 , of a cylinder with radius 5 cm and height 8 cm

[1 mark]

40π

80π

200π

1600π

A cylinder is similar to a prism, so volume = cross-sectional area x length
The cross section is a circle and the length is the height
 $\pi \times 5^2 \times 8 = (25 \times 8)\pi = 200\pi$

- 3 Simplify $16a^2 \div a + 3a \times 2$
Circle your answer.

[1 mark]

$22a$

$8a$

$38a$

$2a$

Follow the order of operations (BIDMAS).
Division is first, then multiplication, then addition.
 $16a^2 \div a = 16a$
 $3a \times 2 = 6a$
 $16a + 6a = 22a$



4 Circle the value of $\cos 30^\circ$

[1 mark]

$\frac{1}{2}$

$\frac{\sqrt{3}}{2}$

0

1

The angles we need to remember are 0, 30, 45, 60 and 90. List these out then write 4, 3, 2, 1 and 0 under them. Square root them and put them over 2

0 30 45 60 90
4 3

5 Work out $8\frac{1}{2} \div 2\frac{2}{3}$

Give your answer as a mixed number.

[4 marks]

$\frac{17}{2} \div \frac{8}{3}$

Converted into improper fractions by multiplying the whole number by the denominator then adding the result to the numerator

$\frac{17}{2} \times \frac{3}{8}$

Divide by a fraction by using 'keep, change, flip'

17

 $\times 3$ $\frac{51}{2}$

$\frac{51}{16}$

Multiply the fractions by multiplying the numerators and denominators together

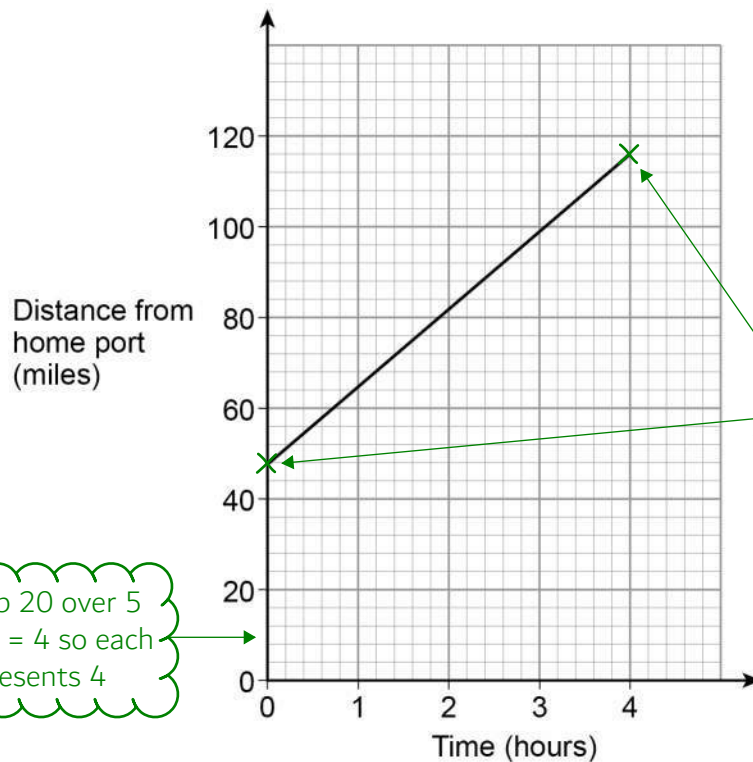
16, 32, 48, 64

Listing out the multiples of 16 to work out how many lots of 16 go into 51. 3 lots fit in with a remainder of 3

Answer

 $3\frac{3}{16}$ 

- 6 A ship is sailing in a straight line from its home port.
The distance-time graph shows 4 hours of the journey.



The scale goes up 20 over 5 small boxes. $20/5 = 4$ so each small box represents 4

The ship started at a distance of 48 miles and finished at 116 miles

Work out the speed of the ship during these 4 hours.

[3 marks]

$$\begin{array}{r} 116 \\ - 48 \\ \hline 68 \end{array}$$

This works out the number of miles travelled during the 4 hours

Answer 17 mph

Miles per hour so we need to divide the miles by the hours

$$4 \overline{) 68}$$



7 The sum of the angles in any quadrilateral is 360°

For example, in a rectangle $4 \times 90^\circ = 360^\circ$

Zak writes,

$$5 \times 90^\circ = 450^\circ \text{ so the sum of the angles in any pentagon must be } 450^\circ$$

Is he correct?

Tick a box.

 Yes

 No

Show working to support your answer.

[2 marks]

$$\begin{array}{r} (5-2) \times 180 \\ \hline 180 \end{array}$$

Sum of interior angles = $(n - 2) \times 180$, where
n is the number of sides of the polygon

$$\begin{array}{r} \times \quad 3 \\ \hline 540 \\ \hline \end{array}$$

Turn over for the next question



- 8 Kim works at an airport in the UK.
She records the number of planes landing between 10 am and 2 pm each day.
The table shows the data for the first 10 days in January.

Day	1	2	3	4	5	6	7	8	9	10
Number of planes	148	151	147	155	153	147	155	102	151	154

- 8 (a) The airport was affected by fog on one of the days.

Which day do you think it was?
Give a reason for your answer.

[1 mark]

Day 8

Reason It is an outlier

All of the other days are around 150. Day 8 isn't close to this

- 8 (b) Kim uses the data to predict how many planes will land at the airport in a year.

In her method, she

uses an estimate of 150 planes in each 4-hour period throughout the day
assumes the same number of planes each day.

Work out her prediction.

[3 marks]

$$\begin{array}{r}
 150 \\
 \times 6 \\
 \hline
 900
 \end{array}$$

There are 24 hours in a day. $24/4 = 6$ so there are 6 4-hour periods each day. This works out that there are 900 planes each day

$$\begin{array}{r}
 365 \\
 \times 900 \\
 \hline

 \end{array}$$

There are 365 days in a year

Answer 328500



- 8 (c)** In fact,
fewer planes land in winter than in summer
fewer planes land at night than during the day.

What does this tell you about Kim's prediction?

Tick **one** box.

Her prediction is too low

Her prediction is too high

Her prediction could be too low or too high

Give a reason for your answer.

[2 marks]

Fewer in winter means it could be too low. Fewer at night means it could be too high.

The prediction was based on the data collected from 10am to 2pm in January. This is in the day and in the Winter

Turn over for the next question



9

$$\sqrt{6^2 + 8^2} = \sqrt[3]{125a^3}$$

Work out the value of a .**[4 marks]**

$$\begin{array}{r} 36 \\ + 64 \\ \hline 100 \end{array}$$

$$6^2 = 36 \text{ and } 8^2 = 64$$

$$\begin{array}{r} 100 \\ \hline 10 = 5a \end{array}$$

The square root of 100 is 10. The cube root of 125 is 5 and the cube root of a^3 is a

Dividing both sides by 5 gets $2 = a$

Answer

2

10

Work out the percentage increase from 80 to 280

[3 marks]

$$280 - 80 = 200$$

Working out the increase

$$\frac{200}{80} = \frac{20}{8} = \frac{10}{4} = \frac{250}{100}$$

Expressing the increase as a fraction of the original then simplifying the fraction (by dividing the numerator and denominator by the same amount) until the denominator is 4, which can be multiplied by 25 to get 100

Answer

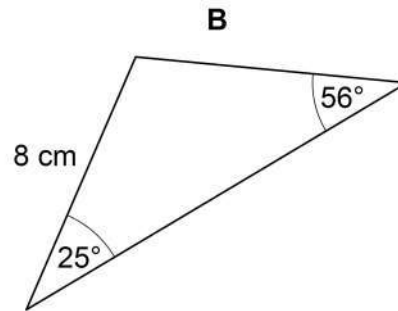
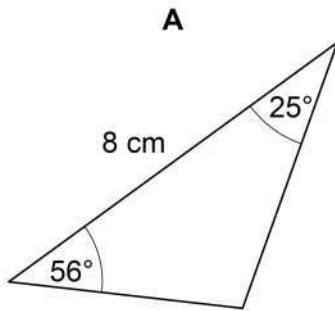
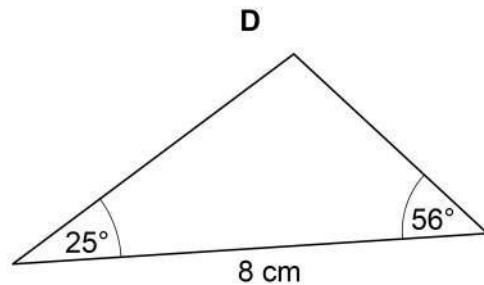
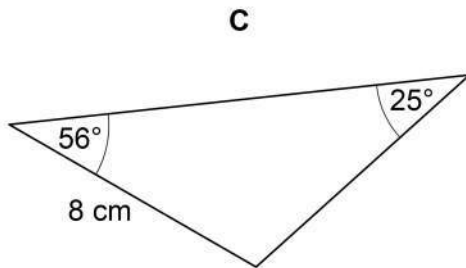
250

%



11

Here are four triangles.

Not drawn
accuratelyWhich **two** triangles are congruent?Circle **two** letters below.

[1 mark]

 A B C D

All the triangles have the same angles and a side of 8cm. But the 8cm is opposite the unknown angle in A and D so these must be the congruent ones

Turn over for the next question

Turn over ►



12 Solve $x^2 - x - 12 = 0$

[3 marks]

$$1 \times 12, 2 \times 6, 3 \times 4$$

Looking for two numbers which multiply to -12 and add to -1. Listing out the factor pairs of 12 until they add to -1 (when one of the pair is negative in order to multiply to a negative)

$$(x+3)(x-4) = 0$$

Factorising the left side

Either $x + 3 = 0$ or $x - 4 = 0$ (as the only way of multiplying two brackets together and getting 0 is if one of them is equal to 0). Rearranging gives these solutions

Answer $x = -3, x = 4$

13 $e:f = 2:3$ and $f:g = 5:4$

Work out $e:g$

Give your answer in its simplest form.

[3 marks]

$$10:15:12$$

Combining the ratios together into the ratio $e:f:g$. f is in common to both ratios so they must have the same number of parts for f in order to be compatible. 15 is a common multiple of 3 and 5. Multiplying both sides of the ratios by the same amount converts them. The 3 parts for f are multiplied by 5 to get 15 so the 2 parts for e also need to be multiplied by 5 to get 10. The 5 parts for f are multiplied by 3 to get 15 so the 4 parts for g also need to be multiplied by 3 to get 12

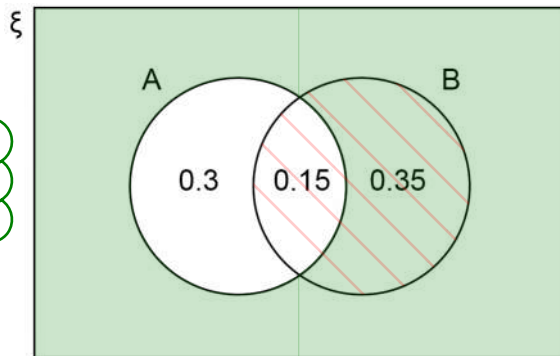
The ratio $e:g$ is $10:12$ and this can be simplified by dividing both sides by 2

Answer $5 : 6$



14 A and B are two events.

Some probabilities are shown on the Venn diagram.



A' is highlighted in green. B is lined in pink. The union is any part which is highlighted or lined

Work out $P(A' \cup B)$

[2 marks]

$$1 - 0.3$$

As everything apart from 0.3 is in the union and the probabilities must add up to 1 (because it is certain that the event A happens or not and that the event B happens or not), this finds the probability

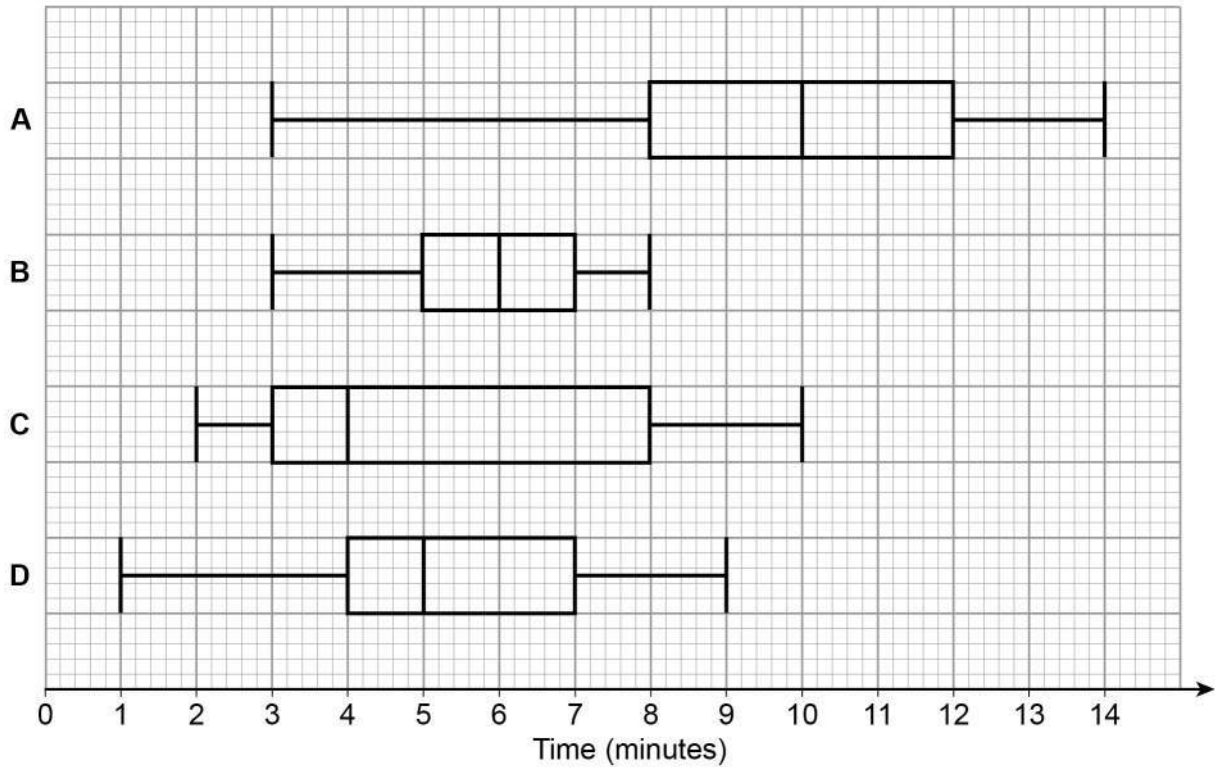
Answer 0.7

Turn over for the next question



- 15** In a survey, queuing times at supermarket checkouts were recorded. One morning, samples of 50 customers were taken at supermarkets A, B, C and D. The box plots represent the results.

Queuing times



- 15 (a)** On average, which supermarket had the lowest queuing times?
Give a reason for your answer.

[2 marks]

Supermarket CReason Lowest median

- 15 (b) At which supermarket were the queuing times most consistent?
Give a reason for your answer.

[2 marks]

Supermarket BReason Lowest interquartile range

- 16 Circle the number that is closest to the value of 29^3

[1 mark]

27 000

90

2700

9000

An estimate is 30^3
 $3^3 = 27$ so $30^3 = 27 \times 10^3$

- 17 Work out the exact value of $\left(\frac{3}{4}\right)^{-3}$

[2 marks]

 $\frac{27}{64}$

First cubing 3 and 4, ignoring the
negative part of the power for now

The negative means the reciprocal
(flip the fraction in this case)

Answer $\frac{64}{27}$

Turn over for the next question

Turn over ►



18

Beth and Mia translate documents from Spanish into English.

A set of documents that would take Beth 8 days would take Mia 10 days.

Beth starts to translate the documents.

After 2 days Beth and Mia both work on translating the documents.

How many **more** days will it take to complete the work?

You **must** show your working.

[4 marks]

$$1 - \frac{2}{8} = \frac{6}{8}$$

As it would take Beth 8 days, she would complete $\frac{1}{8}$ of the documents per day. In two days she would have completed $\frac{2}{8}$. Subtracting this from 1 set of documents leaves $\frac{6}{8}$ of the documents which are still left to be translated

$$\frac{1}{8} + \frac{1}{10} = \frac{10}{80} + \frac{8}{80} = \frac{18}{80}$$

As it would take Mia 10 days, she would complete $\frac{1}{10}$ of the documents per day. Adding together the amounts of documents they complete each day gives the total amount of documents completed each day when both Beth and Mia are working on them

$$\frac{6}{8} \div \frac{18}{80} = \frac{6}{8} \times \frac{80}{18}$$

Time = distance/speed. Distance is basically how much of the documents still need to be translated. Speed is basically how much of the documents are completed each day

Answer $\frac{10}{3}$ days

Cancelling out the 8 with the 80 leaves 10
and cancelling out the 6 with the 18 leaves 3



19 In a chess club, there are x boys and y girls.

19 (a) If 5 more boys and 8 more girls join, there would be half as many boys as girls.

Show that $y = 2x + 2$

[2 marks]

$$x + 5 = \frac{1}{2}(y + 8)$$

$x + 5$ expresses the number of boys there would be in the club.
 $y + 8$ expresses the number of girls there would be in the club.
As the number of boys would be half the number of girls, the number of girls needs to be halved to make them equal

$$2x + 10 = y + 8$$

Multiplying both sides by 2 to get rid of the $\frac{1}{2}$

$$y = 2x + 2$$

Subtracting 8 from both sides makes y the subject and gets what we are trying to show

19 (b) If instead,

10 more boys and 1 more girl join, there would be the same number of boys and girls.

Work out x and y .

[3 marks]

$$x + 10 = y + 1$$

$x + 10$ expresses how many boys there would be. $y + 1$ expresses how many girls there would be. These expressions are equal as there would be the same number of boys and girls

$$= 2x + 2 + 1$$

Substituting y for $2x + 2$ as $y = 2x + 2$

$$7 = x$$

Subtracting x and $(2 + 1)$ from both sides

$$y = 2(7) + 2$$

Substituting 7 for x in $y = 2x + 2$

$$x = \underline{\quad 7 \quad}$$

$$y = \underline{\quad 16 \quad}$$

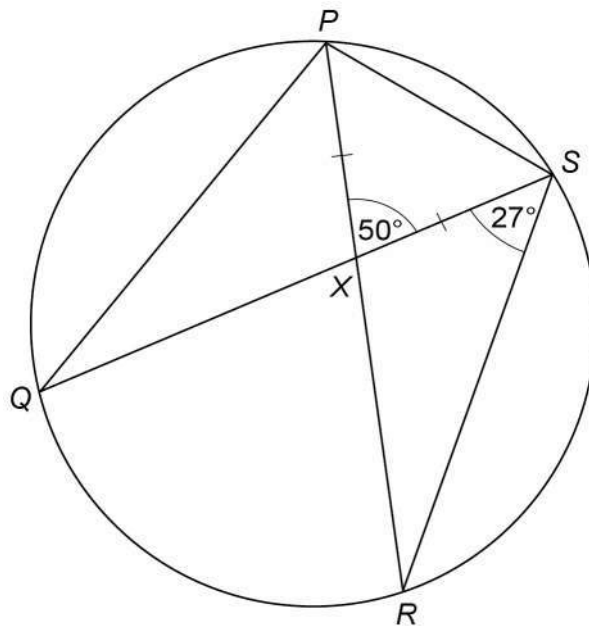


20

P, Q, R and S are points on a circle.

PXR and QXS are straight lines.

$PX = SX$



Not drawn
accurately

Prove that QS is **not** a diameter of the circle.

[4 marks]

Angle $QPR = 27$ as angles in the same segment are equal.

Angles $QPR = QSR$

Angle $XPS = 65$ as there are 180 degrees in a triangle and base angles of an isosceles

triangle are equal.

180 - 50 works out that there are 130 degrees left in triangle XPS . Dividing 130 by 2 gives 65, which is the base angles of the isosceles triangle XPS

Angle $QPS = 92$ so QS is not a diameter as angles in a semicircle are 90 degrees.

Adding angles QPR and XPS gives angle QPS . Angle QPS must be 90 degrees if it is in a semicircle. QS would be the diameter of the semicircle



21

Here are the first four terms of a quadratic sequence.

11	15	26	19	45	68
2		8			
9		18			

Work out an expression for the n th term.**[3 marks]**

The quadratic sequence will be in the form $an^2 + bn + c$.

The difference between 11 and 26 is 15. The difference between 26 and 45 is 19.
The second difference (difference of the 15 and 19) is 4. Halving the second difference gives 2, which is a .

Listing the first two terms of $2n^2$ gives 2 (as $2(1)^2 = 2$) and 8 (as $2(2)^2 = 8$). The difference between 2 and 11 is 9 and the difference between 8 and 26 is 18. This forms a sequence which needs to be added to $2n^2$ to get the original.

The sequence 9, 18 goes up in 9s so must involve $9n$ (so b is 9). The 0th term would be 0 (tracing the sequence backward, it goes down in 9s and $9 - 9 = 0$) so c is 0

Answer _____

$2n^2 + 9n$

Turn over for the next question**Turn over ►**

22

Solve $\frac{x}{x+4} + \frac{7}{x-2} = 1$

You **must** show your working.**[4 marks]**

$$x + \frac{7(x+4)}{x-2} = x+4$$

Multiplying all terms by $(x+4)$
to eliminate it as a denominator

$$x(x-2) + 7(x+4) = (x+4)(x-2)$$

Multiplying all terms by $(x-2)$
to eliminate it as a denominator

$$x^2 - 2x + 7x + 28 = x^2 - 2x + 4x - 8$$

Expanding all the brackets

$$3x = -36$$

Subtracting x^2 from both sides gets rid of the x^2 terms.
Bringing all the x terms to the left side: $-2x + 7x + 2x - 4x = 3x$.
Bringing the constants to the right side: $-8 - 28 = -36$

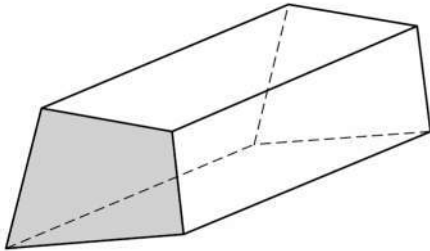
Dividing both sides by 3 gets x on its own. $-36/3 = -12$

$$x = \underline{\quad -12 \quad}$$

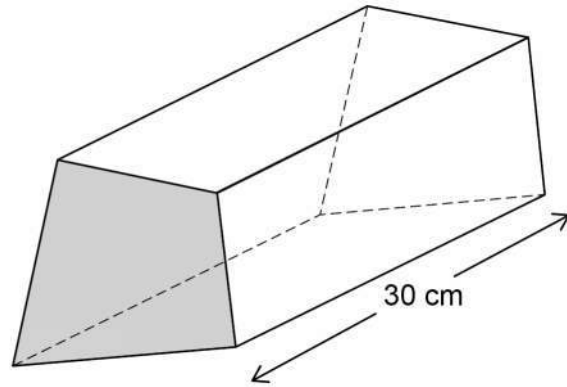


23 Prisms A and B are similar.
The cross sections are shaded.

Prism A
volume = 480 cm^3



Prism B
length = 30 cm



area of the cross section of A : area of the cross section of B = 4 : 9

Work out the area of the cross section of B.

[5 marks]

2 : 3

Area is a squared dimension so square rooting 4 : 9 gives the ratio of the lengths

8 : 27

Volume is a cubed dimension so cubing 2 : 3 gives the ratio of the volumes

$480 \div 8 = 60$

8 parts of the volume ratio represent 480 cm^3 so dividing by 8 works out 1 part. $48/8 = 6$ so $480/8 = 60$

27
 x 60
1620

1 part of the volume ratio is 60 cm^3 so multiplying by 27 works out 27 parts, which is the volume of B

Answer _____ cm^2

54
 $3 \overline{) 162}$

Volume of a prism = (cross sectional area) x length
Cross sectional area = (volume of a prism)/length
Volume of the prism is 1620 cm^3 and it's length is 30.
 $1620/30$ simplifies to $162/3$



24

Show that $\frac{2\sqrt{6}}{\sqrt{5}} - \frac{\sqrt{3}}{\sqrt{10}}$ can be written in the form $\frac{c\sqrt{d}}{10}$

where c and d are integers.

[3 marks]

$$\frac{2\sqrt{30}}{5} - \frac{\sqrt{30}}{10}$$

Rationalising both of the denominators. Multiplying both the numerator and denominator of the first fraction by $\sqrt{5}$ and the second by $\sqrt{10}$

$$\frac{4\sqrt{30} - \sqrt{30}}{10}$$

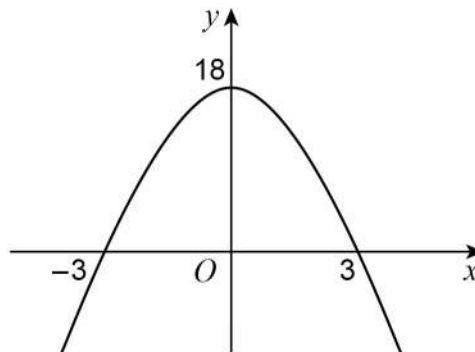
Multiplying the numerator and denominator of the first fraction by 2 to make the denominators the same then combining the fractions with the numerators subtracting

$$\frac{3\sqrt{30}}{10}$$

$4x - x = 3x$, so $4\sqrt{30} - \sqrt{30} = 3\sqrt{30}$



25

A quadratic curve intersects the axes at $(-3, 0)$, $(3, 0)$ and $(0, 18)$ Not drawn
accurately

Work out the equation of the curve.

[3 marks]

$$18 = a(0)^2 + b(0) + c$$

The equation is a quadratic so must be in the form $y = ax^2 + bx + c$.
Substituting in the coordinates of $(0, 18)$ gives this. So $c = 18$

$$0 = a(3)^2 + b(3) + 18 = 9a + 3b + 18$$

$$0 = a(-3)^2 + b(-3) + 18 = 9a - 3b + 18$$

Substituting in the coordinates of
 $(3, 0)$ and $(-3, 0)$ and 18 for c

$$6b = 0$$

$$9a = -18$$

Solving the equations simultaneously by
subtracting them to eliminate the a terms. $b = 0$.
Substituting 0 for b gives $9a = -18$. $a = -2$

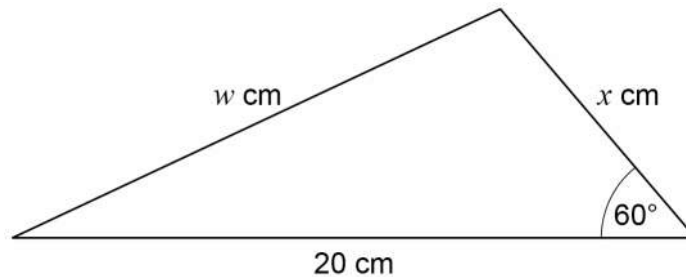
Answer $y = -2x^2 + 18$

Turn over for the next question

Turn over ►



26

The area of this triangle is $25\sqrt{3} \text{ cm}^2$ Not drawn
accuratelyWork out the value of w .Give your answer in the form $a\sqrt{b}$ where a and b are integers greater than 1**[5 marks]**

0	30	45	60	90
0	1	2	$\frac{\sqrt{3}}{2}$	
4	3	2	$\frac{1}{2}$	

Working out the values of $\sin 60$ and $\cos 60$. Listing the angles we need to remember (0, 30, 45, 60, 90) then listing 0, 1, 2, 3, 4 under for the sin values and 4, 3, 2, 1, 0 for the cos values. Square rooting (the square root of 1 is 1 so it doesn't change) then putting them over 2

$$\frac{1}{2} \times 20 \times x \times \frac{\sqrt{3}}{2} = 25\sqrt{3}$$

Area of triangle = $\frac{1}{2} ab \sin C$. Substituting 20 for a , x for b and $\frac{\sqrt{3}}{2}$ for $\sin C$

$$x = 5$$

The $\sqrt{3}$ cancels from both sides (by dividing both sides by it). $\frac{1}{2} \times 20 \times x \times \frac{1}{2} = 5x = 25$. Then dividing both sides by 5 gets x on its own

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\begin{aligned} w &= \sqrt{20^2 + 5^2 - 2 \times 20 \times 5 \times \frac{1}{2}} \\ &= \sqrt{425 - 100} \\ &= \sqrt{325} \end{aligned}$$

The cosine rule can be used to find side w (the sine rule can't be used as there isn't opposite pairs of sides and angles). Rearranging to make a the subject by square rooting both sides then substituting in 20 for b , 5 for c and $\frac{1}{2}$ for $\cos A$

$$25 \sqrt{13}$$

Simplifying into the form $a\sqrt{b}$ by finding a square number which goes into 325. 25 goes in 13 times so using the rule $\sqrt{a} \times \sqrt{b} = \sqrt{ab}$ in reverse allows us to split it into $\sqrt{25 \cdot 13}$

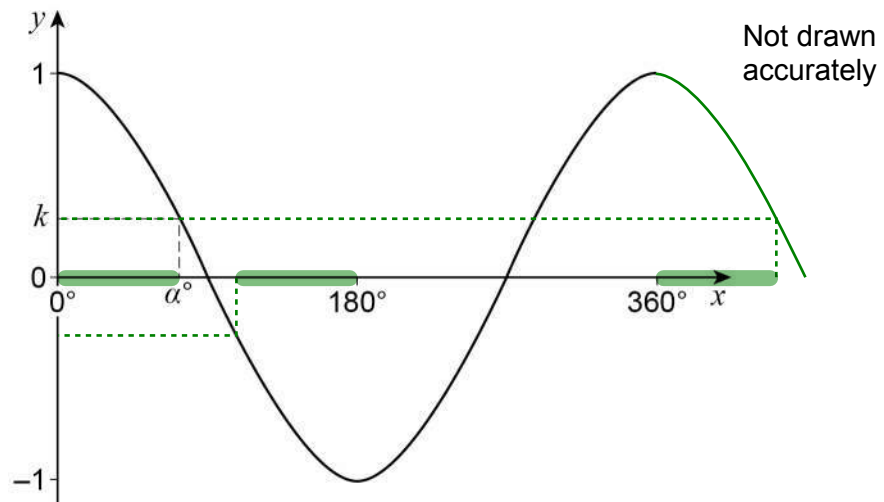
$$\sqrt{25} = 5$$

Answer

$$5\sqrt{13}$$



27 Here is a sketch of $y = \cos x$ for values of x from 0° to 360°



α° is an acute angle.

$$\cos \alpha^\circ = k$$

27 (a) Circle the value of $\cos(180^\circ - \alpha^\circ)$

[1 mark]

$1 - k$

k

$-k$

$-1 - k$

All the distances highlighted in green are the same. The curve is the same from 0 to 90 degrees as 90 to 180 degrees, except it is negative

27 (b) Circle the value of $\cos(360^\circ + \alpha^\circ)$

[1 mark]

$k - 1$

$k + 1$

$-k$

k

All the distances highlighted in green are the same. The curve repeats after 0 to 360 in the same way

END OF QUESTIONS

